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The Power and Joy of Hands-on Numeracy www.toptenmaths.com

Recommended for Year 5

Rounding and Number Lines

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Planning Package

Sequential units with hands-on, real-life numeracy for Year 3, Year 4, Year 5 and Year 6 students

Ten years of development in Australian classrooms.

Genuinely high engagement and conceptual understanding in middle to upper primary numeracy.

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Comprehensive differentiation for wide ranges: Pre-planned and workable enabling and extending prompts for every lesson.

High-impact, high-relevance professional learning on a daily basis to support planning.

Comprehensive diagnostic and formative assessments to target each sequential point-of-need.



Teaching Tips – Rounding

Avoid 'rounding rollercoasters' or 'rounding mountains' and instead repeat this critical question: **"What is it closer to?"** This is best illustrated, solved and proven using a number line.



Rote rules relating to underlining the place next door, and so on, often falter in students' memories when they are conceptually challenged, and also do not create genuine number sense in terms of number line awareness. These fragile procedures frequently fall to pieces when students are asked to round inside a place value (rounding a tens of thousands number to the nearest ten), or estimate while operating, as the rules are too fragile to be applied meaningfully and with a number sense that is critical for real-life numeracy.

Research quoted by Clarke et al (2008): According to this large-scale study, if we do not teach or emphasise rounding and estimation throughout the year of numeracy, we are setting students up to fail in more than 60 percent of real-life scenarios.

The discussion point then becomes the '5,' as it lies in the centre of the number line, so does not appear to be visually closer to either side. There is a reason 5 rounds up – what do you think? (Take some thinking time before reading on...).

Surveys completed by two hundred adults over a twenty-four-hour period found that more than 60 percent of all calculations carried out in daily life only required an estimate (Northcote and McIntosh 1999). We believe that the curriculum emphasis should reflect this finding. This is one reason why teaching fraction algorithms for the four operations does not prepare students for reallife encounters with fractions, where mental estimation is the key skill.

The reason that 5 rounds up is not simply by rule/convention the resumation is the key skill. – there is a mathematical basis for it. How many digits are there? There are 10 digits, including zero. So if we count on one hand – 5 digits go down, and 5 go up. That is an even or fair share for situations in life when we round down, and others when we round up.



Warm-up Games

Warm-ups Climb the Ladder

Focus: Ordering numbers and placing them strategically on vertical number lines



Students fold an A4 page into tenths, twelfths (thirds, then half and half again), or eighths (half, half then half again). Play tenths at first to make the strategy easier to grasp. In the top tenth, write in '1 000 000.' In the bottom tenth, write '0.' Students then roll 6 x 10-sided dice (or pull 6 cards with picture cards removed) and place the number formed somewhere on the their board. Students can rearrange the dice, before writing the number on their board, but the numbers must be placed in order and **are locked in once written**.

The goal is to place numbers in order so that the full 'ladder' is complete. If they roll a number that cannot be placed in their ladder, they miss a turn		
1,000,0000	1,000,000,0	
988,741	82 4,464	
77 6,65	643,221	
682,083	. 617,9 58	
391,607	. 4 96000	
381,636	476,400	
105,795	339,840	
036,263	222,296	
033,468		
0	0 0	

At the end of each game, mark all the numbers they rolled on a number line from 0 to 100 000 (drawing '0' at the start of the A4 page and '1 000 000' at the end).



Check where each number should have actually gone by multiplying each number by 0.00021 using a calculator. For example, for 34 065 x 0.00021, it would go at the 7.15cm mark from the left-hand side of the page. In this way, students can reflect on whether they placed two numbers on their vertical number line too close together. That may be the reason that it was more difficult for them (compared to their partner) to finish the ladder without missing too many turns.

Likewise, if two numbers were placed next to each on the ladder but were very far apart, it may have been that there was too large a gap between them, which also could result in many wasted turns.

In this sense, this game involves more strategy and less chance to play and successfully complete first. Student work sample – support versions Version of the game where 10 000 or 1000 is at the top of the ladder: 1000 10,000 865 9,660 747 7,743 615 6,883 482 3,798 390 3,650 112 1,842

10.00 8.65 6.82 5.83 4.86 2.56 1 49 Extension student work sample Decimal version with 10.00 at the top of the ladder.





Place **Estimation Containers** Value Learning intention: Estimate the volume and/or capacity of a Year 5B container within 25% accuracy. Maths vocabulary: estimate (thinking guess), capacity (how much Lesson 1 liquid it can hold when full), volume (the amount of 3-dimensional space that is taken up, often measured in cubes), millilitres, litres, cubic centimetres, 25% (half of half strategy) Lesson summary: Students create estimation containers at their desk, Grea measuring the capacity of their given container. Students then gallery Estimations walk to estimate all containers in the room, aiming to be within 25% container's actual capacity. Materials: Collection of containers. Include ones with mL markings to ensure students can use these to measure answer for their given container. Numeracy

- Access to a tap or drink bottles for students to use water.
- Place value blocks for students to calculate volume, including tens and hundreds, so students can work it out without having to count by ones.
 Post-it notes.

Best set-up: Students create their own container, measuring its capacity or volume (half the students should use water, and the other half use cubes). Then gallery walk to estimate the capacity of their classmates' containers.



Numeracy picture book link – Great Estimations: https://www.y outube.com/ watch?v=xE XBPWQvp10

Real-life link: Careers that rely heavily on estimation https://www.y outube.com/ watch?v=pxU XwLdRGrs

Estimation 180 website: https://estim ation180.co m/days/ Shopping carts (97): https://estimat ion180.com/d ay-135/

Marshmallow jar (44): https://estimat ion180.com/d ay-117/

Eggs (93) https://estimat ion180.com/d ay-122/

Pages in two different books (first book 183, second book 174): https://estimat ion180.com/d ay-105/ and http://www.est imation180.co m/day-106/

Lego pieces (55): <u>https://estima</u> <u>tion180.com/</u> <u>day-193/</u>



Classroom tip: Galleries using water are particularly quick and easy to set up, but it is important to start with larger objects like giant pompoms or marshmallows first, allowing many students at the start of the session to build confidence and the receive immediate feedback on the reasonableness of their estimates at a whole-class level first.









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 Which professions use estimation a lot? (Painters for the amount of paint required, builders to quote a job, tree loppers for green waste costs).



Connecting the ones place value block (1cm³) to millilitres, the hundreds to 100mL and the one thousands cube to 1L (as well as 1kg)

Modelling: Model the meaning of 1mL using a single drop into a container. What would 100mL look like? Show students a 100mL container, or a container filled with 100mL. What would 250mL look like? What about 500mL? What about 1000mL or 1L?

Also model 1 cubic centimetre by connecting this to the ones place value cubes. The ones is a cube, where all three dimensions (length, height and depth) are 1cm, so it is one centimetre cubed.

Finally, connect mL to cm³ by showing students that if a container can hold 100mL, it can also hold 100cm3 (100 ones cubes). Therefore, to estimate in mL, you can also just think about how many place value blocks (or how many layers of ones) the container could hold if the ones cubes were made of liquid.



The container is wet as the student just checked that it fit 1000 millilitres or 1 litre of water, and now is checking that it fits 1000 cubic centimetres or 1 thousands cube.

8. 3°	1000 ml
1000 ml	000
900	800
800	700
700	- 600
600	500
500	400
300	300
200	200

The same container fits 1000mL, and also 1000cm³.

Beware: Containers that create gaps (like orange juice bottles) will not fit the same number of cubic centimetres as millilitres.

For example, this 500mL juice bottle only fit 300 cubes and the 1L only fit 650 cubes:



	Mernda	500mL	
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Whole-Class Mo the 25% Margin	odelling – Pract for Error Toget	ising Estimatio her	n Galleries and
Whole-Class Me the 25% Margin Whole-class pract estimating as a class estimates, using 4 d	odelling – Pract for Error Toget ice: Fill up some co ss. Students must re columns in their grid	ising Estimation ther ontainers with water ecord the reasoning d books.	n Galleries and and practise behind their
Whole-Class Me the 25% Margin Whole-class pract estimating as a class estimates, using 4 of Gallery name	odelling – Pract for Error Toget ice: Fill up some co ss. Students must re columns in their grid Estimate	ising Estimation ther ontainers with water ecord the reasoning books. Reasoning behind your estimate	n Galleries and and practise behind their Answer and within 25%?

Misconception alert: During the whole-class practice, be sure to highlight the classic misconception of wide and short containers v. skinny and tall containers. Students are often biased towards height and underplay width when estimating and comparing volume and capacity.

Estimation Gallevies Exp Gallery En Keason Marshmallars 1 think this because Marshmallars 1 counted the bottom 1 counted the bottom it by the rous 8×4-2 I think this bacques Pom Poms 12×4=48 the bottom rou had raight and there wen roughly think this because 63 Pom Poms for Pans used the althes Hard Pom Poms and it looked lik there were more in this one.



Student Estimation Galleries

Once most students estimates are frequently within 25% of the answer, set them the task of creating their own container for their classmates to estimate. Half the class should use water and half cubes (girls use water, boys use cubes; then switch for the next session).

For cubes, use tens, hundreds and even thousands blocks where possible (not just ones). Fill each container to the very top (its capacity). Name their gallery with a post-it note (e.g. Mila's gallery).

Once students have created their container, filled with water or cubes, work out the answer to its capacity and record this on a post-it note <u>stuck under</u> <u>the desk or hidden under the grip mat</u>. This provides immediate feedback for other students, after they estimate and record their reasoning, which will then improve their estimates going forward to new galleries.

Reflection: What weighs more, 1L or 1000cm³? Place a 1L container on one side of a balance scale and a 1 thousand block on the other. *Note:* Test this before students enter the classroom to ensure the 1 thousand block is correctly weighted (use a wooden one that is not aged). They are equal – both weight 1kg! What weighs more, 1mL of water or 1 cm³ (1 cm cube, a ones cube)? They weigh the exact same – 1 gram! What will be equal to a tens block? What about the hundreds block?



Support 1 – Ignore the percentages: Remove the percentage element, in terms of working out how close their estimate was. Instead, allow them to decide whether the estimate was 'close' or 'way off' – students are usually quite harsh on themselves, so ensure they are allowing themselves a margin of error.

Support 2 – Use benchmark containers as reference points: Carry around a few example containers with them – one container that can carry exactly 100mL and 100cm³, another that can hold 250, and another that holds 1000. These could be placed at the front for other students to use as benchmarks, but support students should have their own that they can carry to each gallery to use as supportive references.

Extension 1: Place a goal of being within 12.5% or 15%, thereby making the percentage calculation more challenging as well.



Place Value Year 5B Lesson 3 YouTube hook –	Rounding Parkour Learning intention: Round numbers to any place value by thinking "What is it closer to?" Maths vocabulary: round (what is it closer to), place value, number line, halfway (1/2), quarter (1/4), three quarter (3/4), benchmarks Lesson summary: Students jump to each part of the rounding parkour templates with a mini figurine, rounding a number to different place
Parkour: <u>https://www.y</u> <u>outube.com/</u> <u>watch?v=NX</u> <u>7QNWEGcNI</u>	values to earn 'parkour' points. Students also use a piece of paper beside the template to create mini number lines to assist the rounding for every place value, one-at-a-time. After completing the <u>template</u> , students place their number on a 1m number line that spans from zero to one million, or 0 to 1 hundred thousand (or less) for support pairs.
<u>&t=3s</u> and <u>https://www.y</u> <u>outube.com/</u> <u>watch?v=Aep</u> <u>wD2PpDO0</u>	 Materials: Rounding parkour templates and plain A4 paper. Students can bring from home – a mini figurine to act as their parkour 'player' or 'character' during these sessions. <i>Alternative:</i> Pokémon counters, Lego people or similar. Playing cards (remove all picture cards, keep aces as ones). 1m string/rulers/pipes. Best set-up: Whole-class model at a desk with materials, including modelling the number line folding and the template with the class doing a few examples together during the first session to practice both simultaneously.
	nearest million O number Nearest hundred thousand 2.00.000 Nearest thousand 188846 Nearest one thousand 190000 190000

Number Line Strategy – "What is it closer to?"

Use a new piece of white A4 paper for each number that students are trying to round. Fold the page into eighths – half, half, half, all horizontally. These will become the number lines for each place value you are trying to round to.

Pull 6 playing cards in any order (use less cards if students are not ready for all place values as yet) to create a starting number. In the top row (first fold), write the number as the heading – 507 823.

For the second row, try rounding to the nearest ten. For example, when rounding 507 823 to the nearest ten, write the ten the number is currently in to the left and the next ten to the right.

Then mark the halfway point (half of that ten). Mark the quarter and three quarter benchmarks also if they help, particularly for the larger place values. Then mark the number along the line and draw an arrow towards which ten it is closer to. Use your parkour player (mini figurine) to check – if their legs were feeling tired from a huge day of parkour, would they want to jump to *that ten* or *that ten*?



Record this on the <u>parkour template</u>, then move your character to the next hexagon and assist them to solve it using the number lines again. Repeat this process for each place value, emphasising the language 'what is it closer to' and 'what one thousands is the number in' and 'what is the next one thousand?'



Students using a strip of paper as a number line to determine which number their playing card number is closest to. Students also jumped their mini character (circled above) around the parkour templates, acting out parkour as they completed each example.



Students placed each number along a 1m number line (1m ruler, 1m string or 1m PVC pipe stuck to the desk). The one metre number lines were set up by challenge level – 0 to 1 billion for extension, 0 to 1 million for mid-range and 0 to 100 000 or 10 000 for support.





















applying rules they have been told to follow. It then becomes easy to confuse which place needs to be rounded and which digit needs to be focused upon. For this reason, leave the 'rounding mountain' or 'rounding rollercoaster' posters in the cupboard until the very last part of this learning intention – or, better yet, encourage students to create their own versions of anchor charts to summarise the understanding that they formed themselves based on place-value, number-line centric questioning and strategies.

Support: Pull less cards to lower the starting numbers, and only focus on the first parts of the template from the top clockwise (rounding to the nearest ten and hundred), crossing out other parts of the template until they feel ready to attempt these.

hundred million 15:341,279,424 625,100,000,000 Ethan ten million 15,391,279,424) 675,100,000, W 675,000,000,000 nearest M 15,391,279,424, 675,186,539,550 nearest nearest million 15,391,279,424 hundred 16,391,279,424, 675,187,000,00 675, 186, 539, 300 number quadrillion 1515,391,274, 15, 541,280, 424,675,186, nearest 000,000,000 nearest hundred 539,347 000,000 one thousand 15,341,274,424 675,186,500,000 thousand 16,391,279,424 675,186,5496 nearest ten thousand 5, 391,279,424 675, 186,540,009 trillion ten billion 15,341,279,424, 15,391,279,425,000,000 Hundred 000,000, ten thillion 15,391,274,424 Hundred 15,391,279,420 700,000,000,000 15,991,279,400,000 000,000,000,000 000,000,000 ten 8 263 218 nearest nearest hundred 900 million 8263 218 263 000 8 number 900 000 8 263 218 nearest nearest 897 one hundred thousand thousand 8 263 219 nearest 2 263 200 ten 000 000. thousand Negwest 8 263 220 Mallin 000 ten million 8 000 000 Neglinest hundred 8260 000 000 8 000 300 000 000

